



NTNU – Trondheim
Norwegian University of
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Model-Based Safety Assessment with AltaRica 3.0

Towards the next generation of methods, concepts and tools for probabilistic safety assessment
(a computer scientist point of view)

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AltaRica 3.0

domain State {WORKING, HIDDEN_FAILURE, DETECTED_FAILURE}

domain Mode {OPERATION, INSPECTION}

block PeriodicallyInspectedComponent

State state(**init**=WORKING);

Mode mode(**init**=OPERATION);

event failure(**delay**=exponential(lambda));

event repair(**delay**=exponential(mu));

event startInspection(**delay**=Dirac(tau));

event completeInspection(**delay**=Dirac(pi));

parameter Real lambda = 1.0e-3;

parameter Real mu = 0.1;

parameter Real tau = 720;

parameter Real pi = 12;

transition

failure: state==WORKING -> state:=HIDDEN_FAILURE;

repair: state==DETECTED_FAILED -> state:=WORKING;

startInspection: mode==OPERATION -> mode:=INSPECTION;

completeInspection: mode==INSPECTION -> {

mode:=OPERATION;

state := **if** state==WORKING **then** WORKING **else** DETECTED_FAILED;

}

end

Agenda

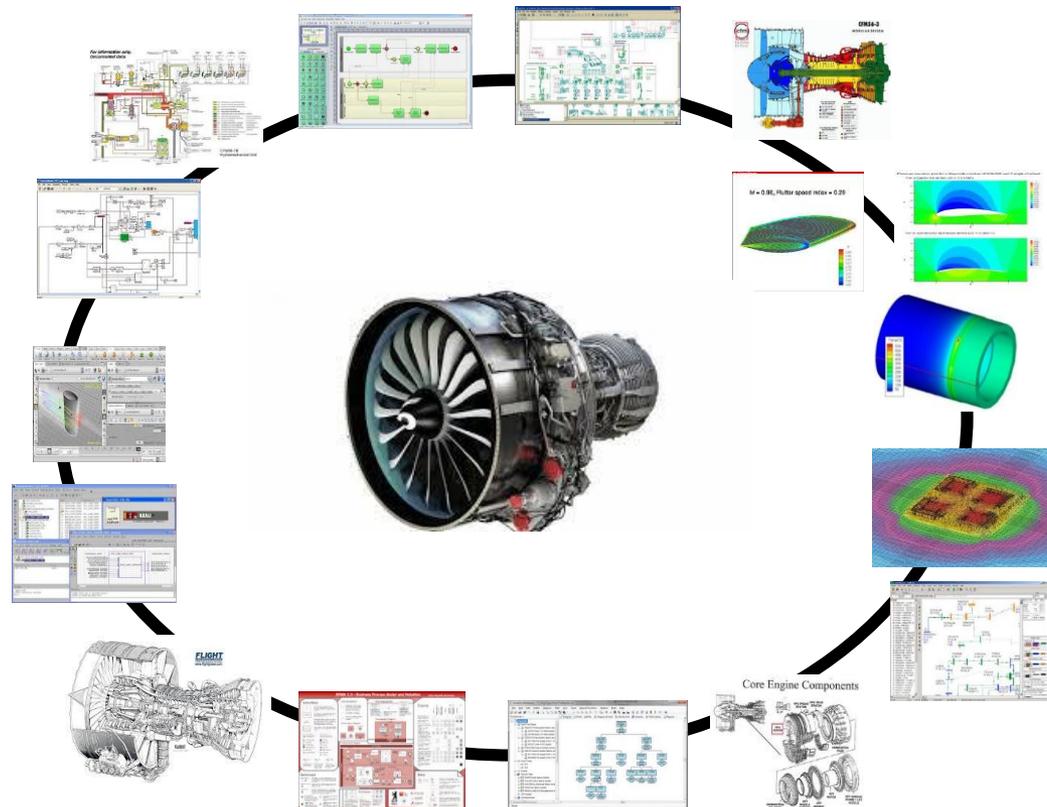
- Rational
- Theses
- Guarded Transitions Systems
- System Structure Modeling Language
- On going and future works

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Model-Based Systems Engineering

How many modeling tools, how many models to design and to operate an aircraft engine?



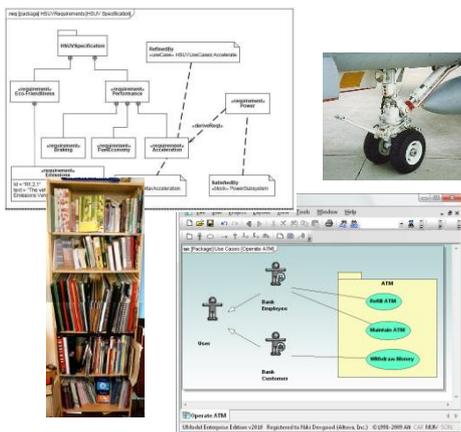
The emerging science of complex systems is the science of models

Today's Challenges of Probabilistic Safety Assessment

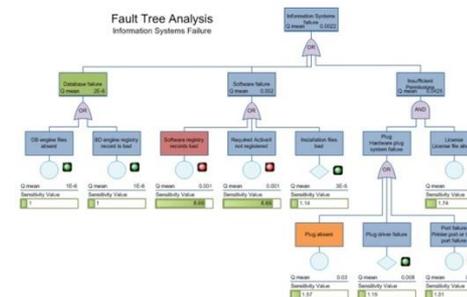
- How to deal with **mechatronics** and **cyber-physical systems** (control mechanisms, reconfigurations...)?
- How to **manage versions and configurations** of models through the life-cycle of systems?
- How to **better integrate** probabilistic risk/safety assessment models with models designed by other engineering disciplines, especially those designed by systems architects.

Issues with “Classical” Safety Models

Systems specifications

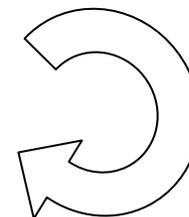


Models



Calculations

- Failure scenarios
- Failure probabilities



Fault Trees, Event Trees, Markov Chains, Stochastic Petri Nets...

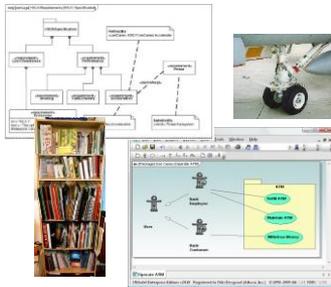
Classical modeling formalisms used for safety analyses lack of expressive power and/or of structure.

- **Distance** between **systems specifications** and **models**;
- Models are **hard to design** and even **harder to share with stakeholders** and to **maintain** throughout the **life-cycle** of systems.
- Often too **conservative** approximations

The Model-Based Safety Assessment promise

Reducing the gap between systems specifications and probabilistic safety assessments

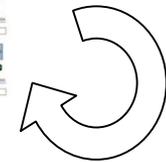
Systems specifications



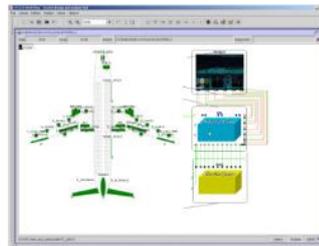
Models



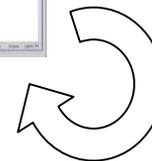
Calculations



High level models
reflecting systems architecture



Calculations



Agenda

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- Theses
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- System Structure Modeling Language
- On going and future works

“In philosophy and rhetoric, a thesis is a statement that can be summarized with a simple sentence, but that is supported by an organized set of hypotheses, arguments and conclusions. It is the position of an author, a school, a doctrine or a movement on a given subject.”

Wikipedia

Thesis 1

Models should not be confused with their graphical representations

Meaning and practical consequences:

- A model is a **mathematical object**.
- A **graphical representation** is a view on the model, very useful for **communication**, but...
- **Complex models cannot be fully represented graphically.**
- Moreover, which **several alternative graphical representations** can be proposed for the same model.

In a word, we have to think first to mathematical objects, then to their possible graphical representations

Thesis 2

A probabilistic safety assessment model results always of a tradeoff between the accuracy of the description of the system under study and the computational cost of calculations of risk/safety indicators

Meaning and practical consequences:

- Calculations of probabilistic indicators are **provably computationally hard** (#P-hard).
- Assessment algorithms perform (unwarranted) **approximations**.
- The more complex the model, the coarser the approximations.
- Adding **more expressive power** is interesting only if it can be done at **low computational cost**.
- Moreover, the more complex the model, the harder its **validation**.

Thesis 3

Behaviors + Structures = Models*

Meaning and practical consequences:

- Any modeling language is the combination of a **mathematical framework** to describe the behavior of the system under study and a **structuring paradigm** to organize the model.
- The choice of the **appropriate mathematical framework** for a model depends on the **characteristics of the system** one wants to study.
- **Structuring paradigms** are to a very large extent **independent** of the chosen mathematical framework. They can be studied on their own.

(*) In reference to Wirth's seminal book "Algorithms + Data Structures = Programs"

AltaRica 3.0

$$\begin{array}{ccccccccc} \text{Behaviors} & + & \text{Structures} & = & \text{Models} \\ \text{GTS} & + & \text{S2ML} & = & \text{AltaRica 3.0} \end{array}$$

GTS: Guarded Transitions Systems

Generalization of state/transitions formalisms such as (multiphase)
Markov chains and stochastic Petri nets

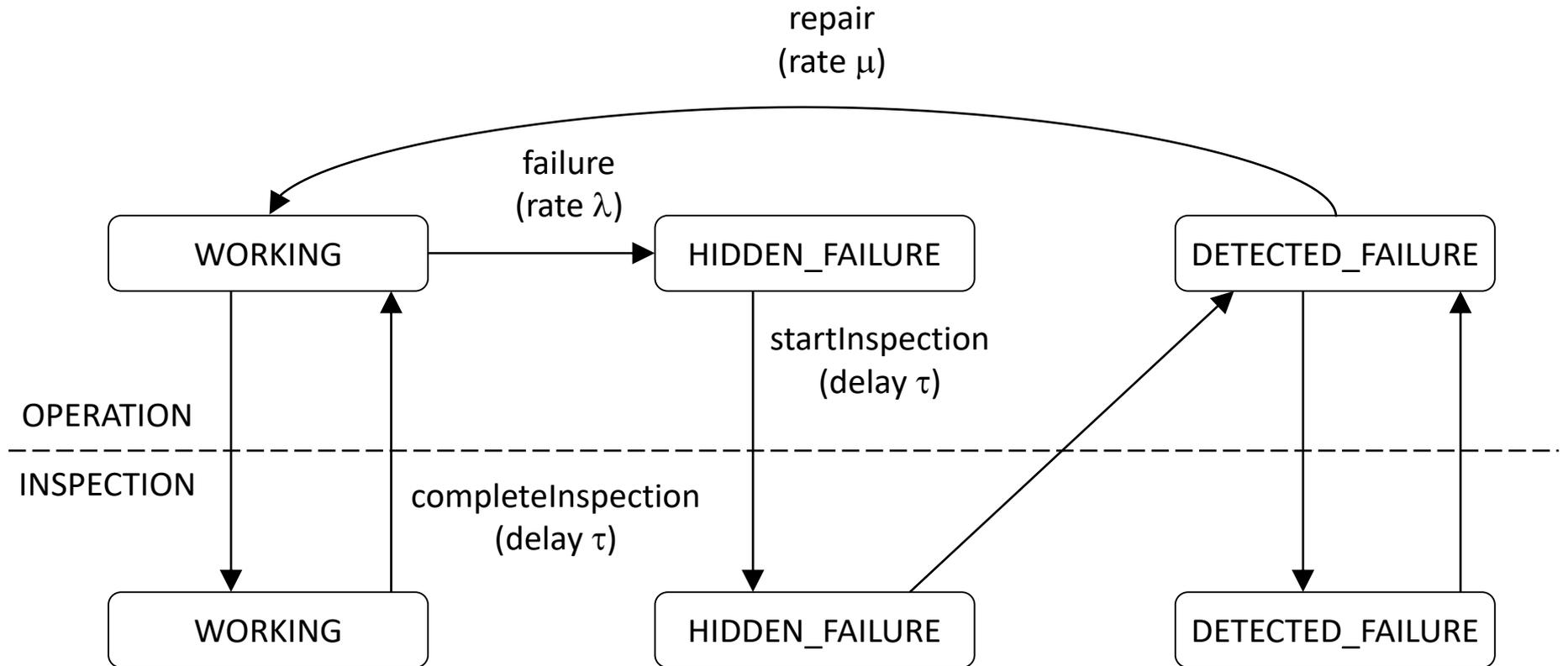
S2ML: System Structure Modeling Language

Sets of structuring mechanisms stemmed from object-oriented
programming

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State, Events and Transitions



Model for a periodically inspected component

Stochastic Discrete Event Systems

domain State {WORKING, HIDDEN_FAILURE, DETECTED_FAILURE}

domain Mode {OPERATION, INSPECTION}

block PeriodicallyInspectedComponent

State state(**init**=WORKING);

Mode mode(**init**=OPERATION);

event failure(**delay**=exponential(lambda));

event repair(**delay**=exponential(mu));

event startInspection(**delay**=Dirac(tau));

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parameter Real mu = 0.1;

parameter Real tau = 720;

parameter Real pi = 12;

transition

failure: state==WORKING -> state:=HIDDEN_FAILURE;

repair: state==DETECTED_FAILED -> state:=WORKING;

startInspection: mode==OPERATION -> mode:=INSPECTION;

completeInspection: mode==INSPECTION -> {

mode:=OPERATION;

state := **if** state==WORKING **then** WORKING **else** DETECTED_FAILED;

}

end

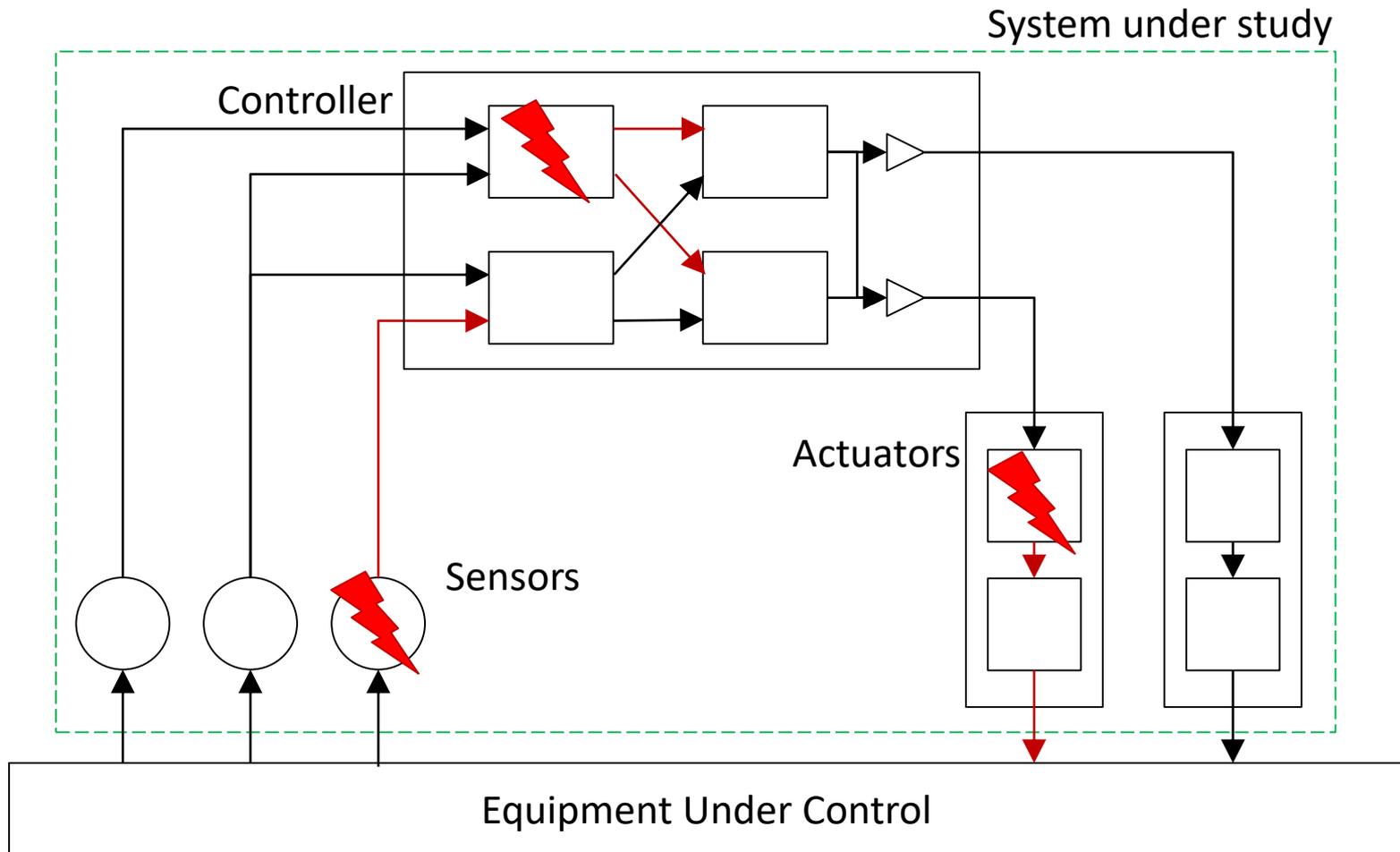
State variables

Events associated with stochastic or deterministic delays

Parameters

Transitions

Flow propagation



Flow propagation

block System

...

block Sensor3

...

Boolean input, output (reset=false),

...

assertion

output := state==WORKING and input;

...

end

...

block Controller

block AcquisitionModule1

...

Boolean input1, input2 (reset=false);

...

end

...

end

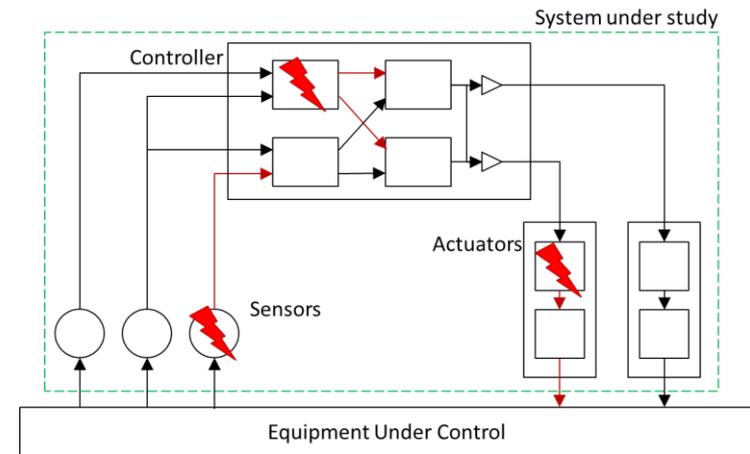
assertion

...

Controller.AcquisitionModule1.input1 := Sensor3.output;

...

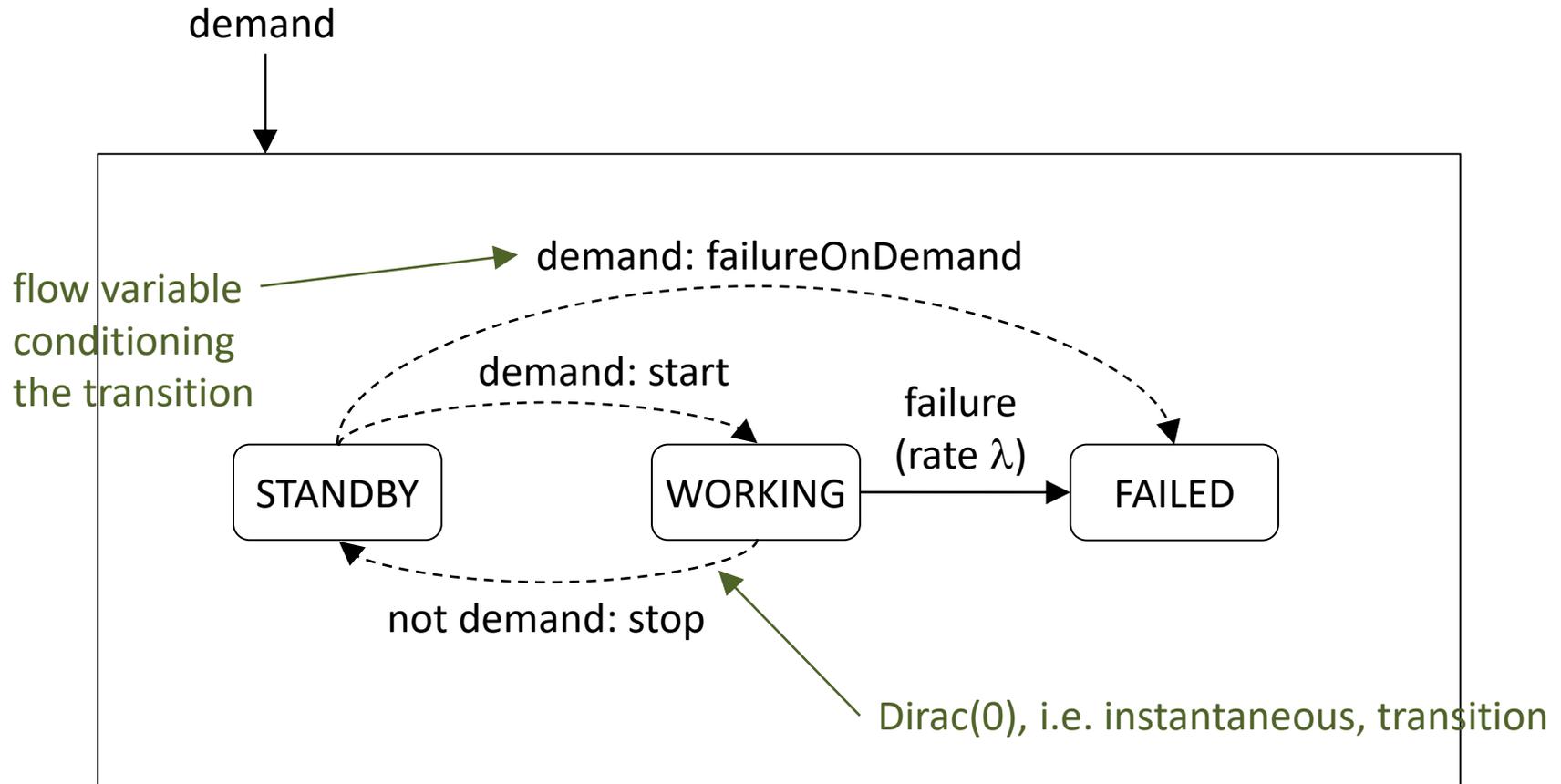
end



Flow variables

Assertions
(transfer functions)

Reusable Modeling Components



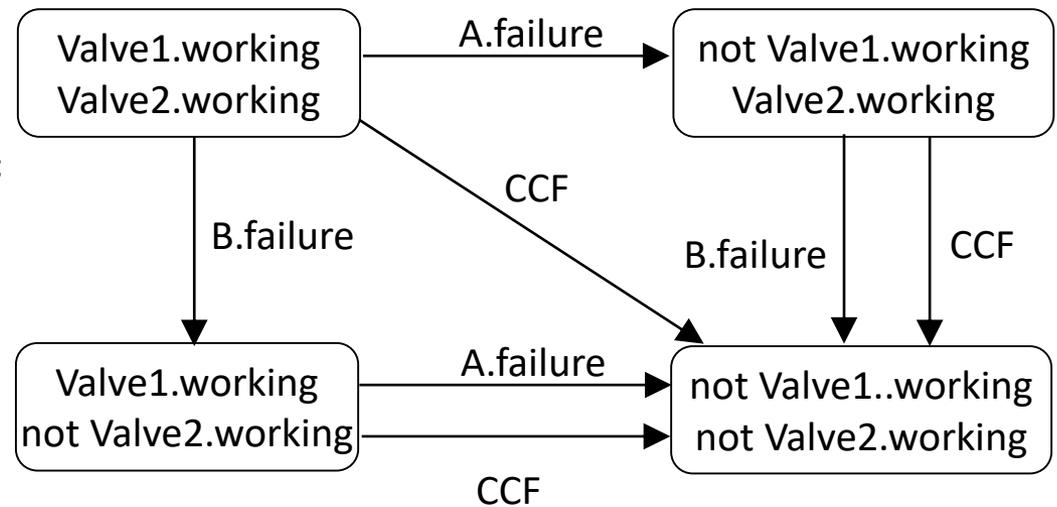
Model for a cold spare component

Synchronization

It is possible to fire several events simultaneously. This is called a **synchronization**.

```
block System
  block Valve1
    Boolean working (init = true);
    event failure;
  transition
    failure: working -> working := false;
    repair: not working -> working := true;
  end
  block Valve2
    ...
  end
  event CCF;
  transition
    CCF: ?Valve1.failure & ?Valve2.failure;
end
```

Model with a common cause failure



synchronization

Formal Definition

A **Guarded Transition Systems** is a quintuple $\langle V, E, T, A, \iota \rangle$, where:

- V is a set of **variables**. V is the disjoint union of the set S of **state variables** and the set F of **flow variables**: $V = S \uplus F$.
- E is a set of **events**.
- T is a set of **transitions**, i.e. of triples $\langle e, G, P \rangle$, where e is an event of E , G is a Boolean expression built on variables of V and P is an instruction built on variables of V . For the sake of the clarity, we shall write a transition $\langle e, G, P \rangle$ as $e: G \rightarrow P$.
- A is an **assertion**, i.e. an **instruction** built on variables of V .
- ι is an assignment of variables of V , so-called initial or **default assignment**.

The set of **instructions** is the smallest set such that.

- “skip” is an instruction.
- If v is a variable and E is an expression, then “ $v := E$ ” is an instruction.
- If C is a (Boolean) expression, I is an instruction, then “if C then I ” is an instruction.
- If I_1 and I_2 are instructions, then so is “ $I_1 ; I_2$ ”.

Formal (Denotational and Operational) Semantics

$$S0: \frac{}{\langle skip, \sigma, \tau \rangle \rightarrow \tau}$$

$$S1: \frac{\tau(v) = ?, \quad \sigma(E) \in dom(v)}{\langle v := E, \sigma, \tau \rangle \rightarrow \tau[\sigma(E)/v]}$$

$$S2: \frac{\tau(v) = \sigma(E), \quad \sigma(E) \in dom(v)}{\langle v := E, \sigma, \tau \rangle \rightarrow \tau}$$

$$S3: \frac{\sigma(E) = ERROR \text{ or } \sigma(E) \notin dom(v) \text{ or } \tau(v) \neq ?, \quad \sigma(E) \neq \tau(v)}{\langle v := E, \sigma, \tau \rangle \rightarrow ERROR}$$

$$S4: \frac{\sigma(C) = TRUE}{\langle \text{if } C \text{ then } I, \sigma, \tau \rangle \rightarrow \langle I, \sigma, \tau \rangle}$$

$$S5: \frac{\sigma(C) = FALSE}{\langle \text{if } C \text{ then } I, \sigma, \tau \rangle \rightarrow \tau}$$

$$S6: \frac{\sigma(C) = ERROR}{\langle \text{if } C \text{ then } I, \sigma, \tau \rangle \rightarrow ERROR}$$

$$S7: \frac{\langle I_1, \sigma, \tau \rangle \rightarrow \tau'}{\langle I_1; I_2, \sigma, \tau \rangle \rightarrow \langle I_2, \sigma, \tau' \rangle}$$

$$S8: \frac{\langle I_2, \sigma, \tau \rangle \rightarrow \tau'}{\langle I_1; I_2, \sigma \rangle \rightarrow \langle I_1, \sigma, \tau' \rangle}$$

$$S9: \frac{\langle I_1, \sigma, \tau \rangle \rightarrow \langle I'_1, \sigma, \tau' \rangle}{\langle I_1; I_2, \sigma, \tau \rangle \rightarrow \langle I'_1; I_2, \sigma, \tau' \rangle}$$

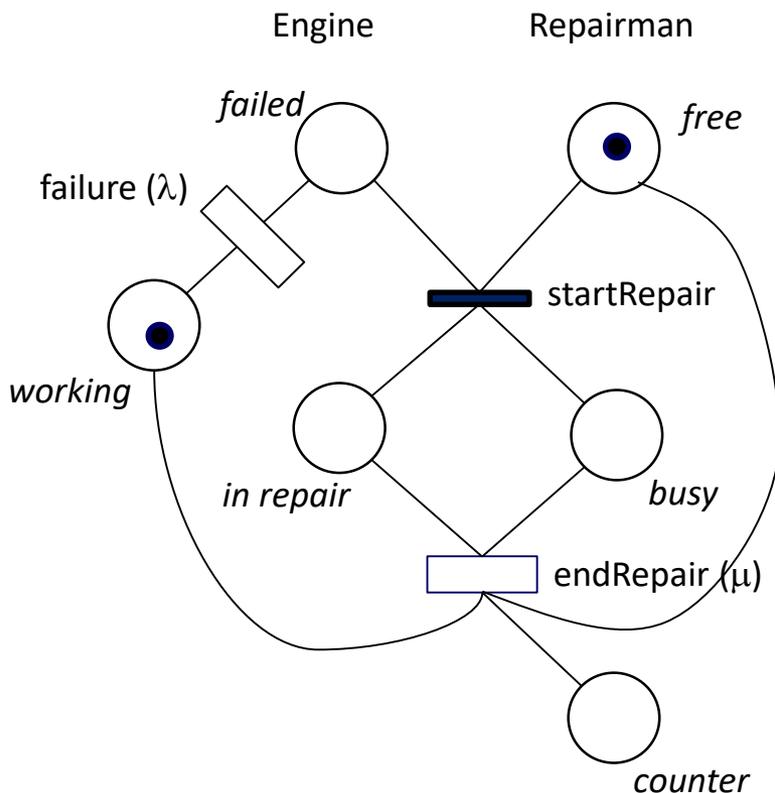
$$S10: \frac{\langle I_2, \sigma, \tau \rangle \rightarrow \langle I'_2, \sigma, \tau' \rangle}{\langle I_1; I_2, \sigma \rangle \rightarrow \langle I_1; I'_2, \sigma, \tau' \rangle}$$

$$S11: \frac{\langle I_1, \sigma, \tau \rangle \rightarrow ERROR}{\langle I_1; I_2, \sigma, \tau \rangle \rightarrow ERROR}$$

$$S12: \frac{\langle I_2, \sigma, \tau \rangle \rightarrow ERROR}{\langle I_1; I_2, \sigma, \tau \rangle \rightarrow ERROR}$$

Comparison with Existing Modeling Formalisms

Guarded transitions systems **generalize at no computational cost** existing modeling formalisms such as Markov chains, Stochastic Petri Nets...



domain EngineState = { WORKING, FAILED, IN_REPAIR }

domain RepairManState = { FREE, BUSY }

block MyNet

EngineState engine (**init** = WORKING);

RepairManState repairMan (**init** = FREE);

Integer counter (**init** = 0);

event failure (**delay** = exponential(lambda));

event startRepair (**delay** = 0);

event enRepair (**delay** = exponential(1mu));

parameter Real lambda = 1.0e-3;

parameter Real mu = 1.0e-1;

transition

failure: engine==WORKING -> engine := FAILED;

startRepair: engine==FAILED and repairMan==FREE -> {
engine := IN_REPAIR; repairMan := BUSY; }

endRepair: engine==IN_REPAIR and repairMan==BUSY -> {
engine := WORKING; repairMan := FREE;
counter:= counter+1; }

end

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Object-Oriented Modeling

```
class PeriodicallyInspectedComponent  
  State state(init=WORKING);  
  Mode mode(init=OPERATION);  
  event failure(exponential(lambda));
```

...

```
end
```

```
class Valve  
  inherits SpareComponent;
```

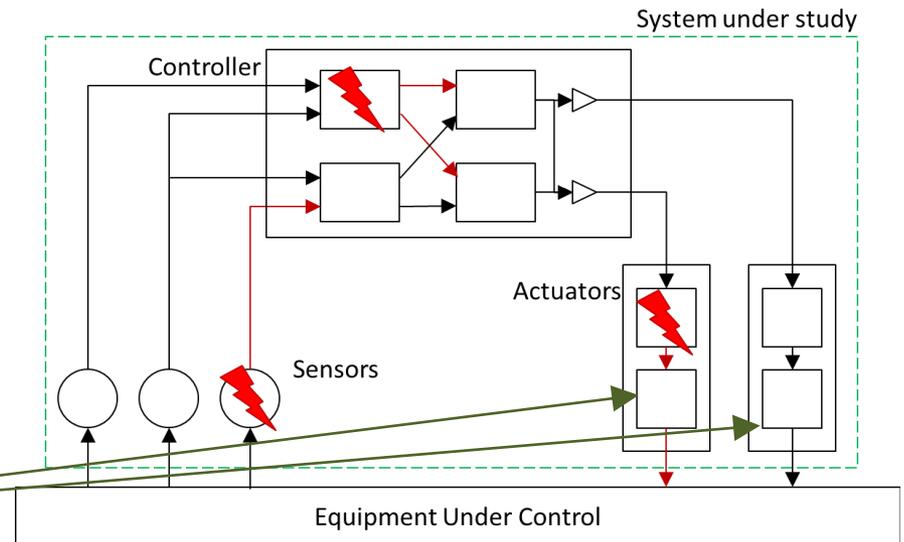
...

```
end
```

```
block SafetyInstrumentedSystem  
  Valve SDV1, SDV2;
```

...

```
end
```



Fundamental objects and relations

S2ML gathers and organizes **fundamental concepts** of modeling languages.

Objects

Ports	variables: state, demand, events: failure...
Containers	block SDV1, class Pump...

Operational relations

Connection	failure: state==WORKING -> state:= FAILED;
------------	--

Hierarchical relations

Composition	pump SDV1 is-part-of of system SIS
Aggregation	system SIS uses power-supply PW

Reuse relations

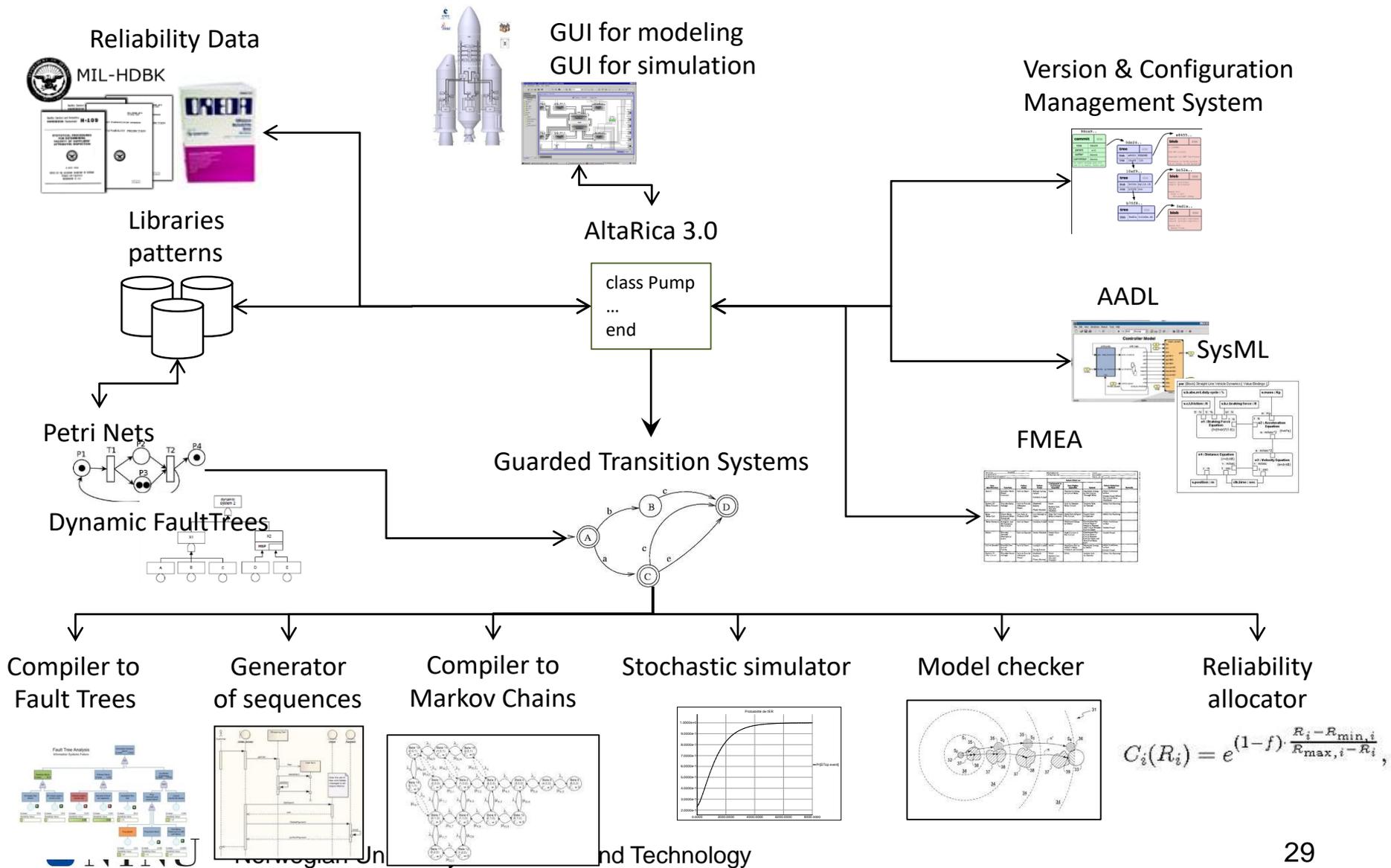
Instantiation	SDV1 is-a-copy-of on-the-shelf component Pump
Inheritance	Pump is-a PeriodicallyInspectedComponent
Cloning	train2 is-a-copy-of train1

Polymorphism

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The AltaRica 3.0 project



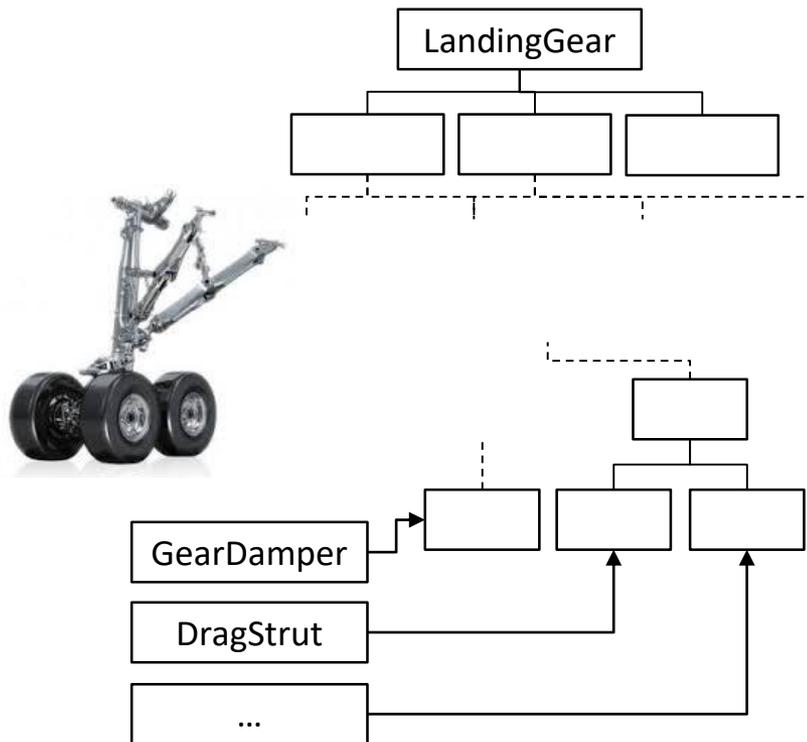
S2ML+X paradigm

Behaviors	+	Structures	=	Models
Guarded Transitions Systems	+	S2ML	=	AltaRica 3.0
Boolean equations	+	S2ML	=	Fault Trees (++)
Markov chains	+	S2ML	=	...
Petri nets	+	S2ML	=	GRIF (++)
Ordinary Differential Equations	+	S2ML	=	Simulink (++) Modelica (++)
Mealy machines	+	S2ML	=	Lustre (++)
Process algebras	+	S2ML	=	Scola
Bayesian networks	+	S2ML	=	...
Requirements	+	S2ML	=	...
...	+	...	=	...

Thesis 4 (Pattern-Based Systems Engineering)

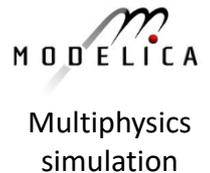
Reuse is the key issue for the efficiency of the modeling process

Meaning and practical consequences:



- Top-down model design
- System level
- Reuse of modeling patterns
- Prototype-Oriented

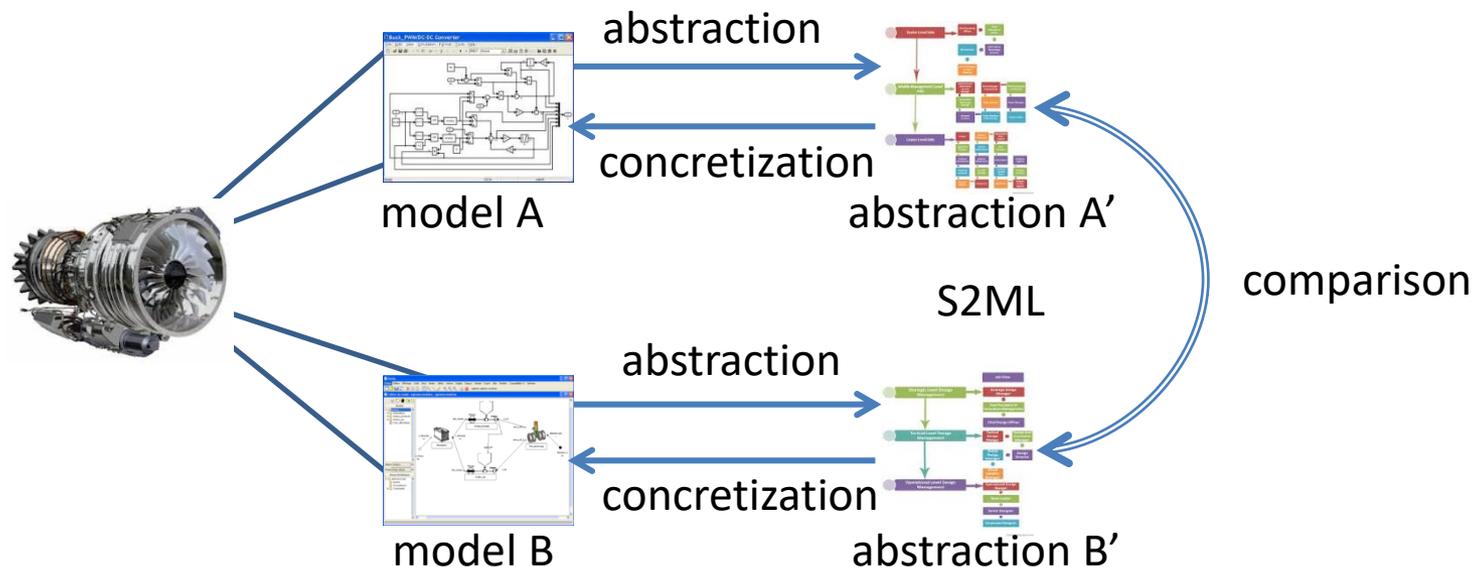
- Bottom-up model design
- Component level
- Reuse of modeling components
- Object-Oriented



Thesis 5 (Model Synchronization)

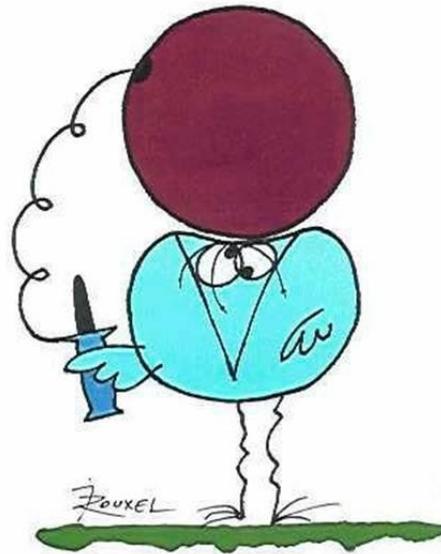
Abstraction + Comparison = Synchronization*

Meaning and practical consequences:



(*) Cousot's abstract interpretation is thus the conceptual framework of model synchronization.

Les devises Shadok



By trying and trying again, you always end up in succeeding. Consequently, the more you fail, the better your chances of success